

Topic 1: Numbers and Algebra

Binomial Expansion

- 1. (a) Expand and simplify $(1-b)^3$ in ascending powers of b.
- (2 marks)

(b) By using a suitable substitution for *b*, show that

$$1 - 3\sin^2 x + 3\sin^4 x - \sin^6 x = \cos^6 x$$

(3 marks)



Mark scheme:

1. (a)
$$(1-b)^3$$

An attempt to use the binomial theorem or simply multiplying (M1)

$$(1-b)^3 = 1 - 3b + 3b^2 - b^3 \tag{A1}$$

(b) If
$$b = \sin^2 x$$
 (A1)

$$1 - 3\sin^2 x + 3\sin^4 x - \sin^6 x = (1 - \sin^2 x)^3$$

$$(1 - \sin^2 x)^3 = (\cos^2 x)^3 \tag{M1}$$

$$(\cos^2 x)^3 = \cos^6 x \tag{A1}$$